

# Spatial Transcriptomic Alignment, Integration, and de novo 3D Reconstruction by STAIR

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## Method Article

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# 1 Spatial Transcriptomic Alignment, Integration, and *de novo* 3D 2 Reconstruction by STAIR

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## 8 9 **Abstract**

10 Spatial transcriptomics (ST) has emerged as a transformative approach for comprehending tissue  
11 architecture with molecular profiles. However, amalgamating discrete two-dimensional (2D) ST  
12 snapshots into a unified 3D atlas remains an outstanding challenge. To this end, we introduce STAIR,  
13 an end-to-end solution for ST alignment, integration, and *de novo* 3D reconstruction. STAIR uses a  
14 heterogeneous graph attention network with spot-level and slice-level attention mechanisms to  
15 obtain a unified embedding space and guide 3D space reconstruction in an unsupervised manner.  
16 We demonstrate STAIR's marked improvements in slice alignment and integration across samples  
17 and platforms over the previous methods. Furthermore, STAIR shows first-of-its-kind performance  
18 in *de novo* 3D reconstruction, with demonstrations in mouse hypothalamus preoptic area, mouse  
19 brain, and breast tumor tissue, which provides precise delineation of brain regions and reveals tumor  
20 progression in 3D space. Additionally, STAIR integrates additional slices into the existing 3D atlas  
21 incorporating both molecular features and physical coordinates. STAIR is the first to address the  
22 core obstacles limiting 3D positioning and harnessing alignments for atlas construction and  
23 assimilation. It lays a computational foundation to construct unified tissue maps and provides novel  
24 biological insights from a 3D perspective.

## 25 26 **Keywords**

27 Spatial transcriptome, *de novo* 3D reconstruction, Alignment, Integration, Heterogeneous graph  
28 attention network

## 29 **Introduction**

30 Recently remarkable advancements have enabled the generation of spatial transcriptomic (ST) data  
31 that captures gene expression with preserved spatial context. Various sequencing techniques<sup>1-7</sup>  
32 facilitate exploring molecular features within tissues from a spatial perspective. To study an organ  
33 or tissue in three-dimensional (3D) space, researchers sampled parallel slices of specific samples at  
34 certain distance intervals, where individual slices capture spatially resolved molecular features in a  
35 single plane<sup>8-10</sup>. At present, construction of ST-based molecular atlases is ongoing, such as mouse  
36 brain<sup>8</sup>, macaque brain<sup>10</sup>, and drosophila embryo<sup>9</sup>. By revealing topological structures organ-wide,  
37 these studies advance our comprehension of molecular drivers of tissue organization.

38 Several computational methods including PASTE<sup>11</sup>, PRECAST<sup>12</sup>, STAligner<sup>13</sup> and STitch3D<sup>14</sup>  
39 have enabled important advancements in handling multi-slice ST data. Specifically, PRECAST<sup>12</sup>  
40 introduced a novel probabilistic approach mainly focusing on spatial embedding integration.  
41 PASTE<sup>11</sup> proposed an innovative method for 2D coordinate alignment by balancing expression and  
42 physical proximity to obtain optimal transport between slices. STAligner<sup>13</sup> made pioneering work  
43 in the unified alignment of both embeddings and coordinates. It first employed graph attention  
44 networks with triplet loss for integrating spatial embeddings, followed by aligning 2D coordinates  
45 based on the selection of landmark domains that are uniformly shaped across slices. While most  
46 methods aligning physical space perform only 2D coordinate registration, more recently, STitch3D<sup>14</sup>  
47 pioneered intriguing 3D analytical capability by jointly modeling multiple slices. It reconstructed  
48 3D views of tissue structures, cell distributions, and developmental trajectories with the requirement  
49 of additional single-cell data.

50 The previous methods such as STaligner and STitch3D utilized known inter-slice distance or  
51 3D coordinates for 3D reconstruction. However, this information can be unavailable or unreliable  
52 when integrating across-sample, across-study sections with non-standardizable slice distances,  
53 severely limiting multi-source 3D assembly. Therefore, computed inference of inter-relationship  
54 positioning is imperative to enable coherent fusion. Regrettably, current solutions do not furnish this  
55 capability. In addition, existing reconstructed atlases also have minimal capacity for quantitative  
56 annotation transfer or assimilation of emerging data, impeding continued knowledge accumulation

57 within fixed spatial references.

58 To address these challenges, we developed STAIR, an integrated solution for end-to-end  
59 alignment, integration, and *de novo* 3D construction. STAIR utilizes heterogeneous graph attention  
60 network<sup>15</sup> to learn spatial embedding, and completes the reconstruction of physical location based  
61 on this. Unlike previous methods relying on known slice distance or known 3D coordinates, STAIR  
62 requires only ST data as input and infers the relative positioning of slices along z-axis in a  
63 completely unsupervised manner. In addition, STAIR seamlessly integrates new slices into the  
64 existing 3D atlas, expanding and updating the reference 3D atlas. We demonstrated STAIR's  
65 superior performance over existing methods for spatial features and 2D coordinates alignment  
66 across various datasets. Furthermore, STAIR was the first-of-its-kind method for *de novo* 3D  
67 reconstruction, with demonstrations of mouse hypothalamic preoptic area, whole mouse brain, and  
68 tumor tissue. Finally, STAIR achieved seamless integration of a new slice from a different ST  
69 platform into a constructed 3D atlas, accurately transferring the annotation information in the atlas  
70 to the new slice. STAIR is publicly available as an open-source Python package at  
71 <https://github.com/yuyuanyuana/STAIR>.

72

## 73 **Results**

### 74 **Overview of the STAIR framework**

75 STAIR achieves integration and alignment of molecular features and physical coordinates for ST  
76 data, enabling 3D reconstruction and assimilation of new slices into the reference atlases (Fig. 1). It  
77 takes only ST data as input and outputs aligned spatial embeddings and coordinates. It comprises  
78 two central modules (Fig. 1A), STAIR-Emb performs embedding alignment, while STAIR-Loc  
79 handles coordinate registration. Spatial domains and developmental trajectories are derived solely  
80 from the aligned embeddings via clustering and trajectory inference, respectively. Thus, relying on  
81 multi-slice data alone, STAIR is capable of *de novo* 3D reconstruction and further obtaining discrete  
82 organizational structures and continuous dynamic relationships in 3D space.

83 For embedding alignment (Fig. 1A, left), an autoencoder with batch factor<sup>16,17</sup> performs

84 nonlinear dimensionality reduction to account for platform-specific effects in gene expression.  
85 STAIR-Emb then constructs a heterogeneous graph with spots across all slices as nodes, and the  
86 node attribution is decided by their original slices. Connectivity for spots in the same slice is defined  
87 by spatial neighborhoods while inter-slice edges are weighted by gene expression affinities from the  
88 encoder output since the relative positions between slices are unknown. Subsequently, STAIR-Emb  
89 employs an attention mechanism<sup>15</sup> consisting of spot-level and slice-level attention for adaptive  
90 information aggregation within and between slices, obtaining low-dimensional spatial features of  
91 spots that encapsulate rich biological signals. In parallel, the attention score produces inter-slice  
92 relationship matrices reflecting higher-order tissue correspondences.

93 For coordinate registration (Fig. 1A, right), STAIR-Loc implements a two-step procedure  
94 between slice pairs. In the initial alignment, rotation, scaling, and translation guided by anchor  
95 correspondences in the embedding produce an approximate overlay. In the fine alignment, STAIR-  
96 Loc employs the Iterative Closest Point (ICP)<sup>18</sup> algorithm for precise registration based on boundary  
97 points of the slices and the most aggregated domain. By sequential application across ordered slices,  
98 this procedure reconstructs a stacked 3D physical map.

99 For a fully unsupervised 3D reconstruction from an arbitrary set of parallel slices (Fig. 1B), z-  
100 axis coordinates are first reconstructed from inter-slice attention scores derived from STAIR-Emb  
101 using a minimum spanning tree (MST)<sup>19</sup>. These predicted z-coordinates are then used to guide x-  
102 axis and y-axis alignment using STAIR-Loc. Post-reconstruction, seamlessly assimilating additional  
103 acquisitions is also enabled (Fig. 1C). The z-coordinate of a new slice is initially predicted by  
104 leveraging attention-based inter-slice proximity scoring to identify the nearest neighboring atlas  
105 slices for weighted positional estimation. The most proximal atlas slice serves as a spatial template  
106 to scale and align the x- and y-coordinates of the new data. At this stage, annotated atlas information  
107 like standard anatomical region labels can be accurately propagated to newly integrated slices. This  
108 continual expansion over time enhances the utility and applicability of an established 3D reference.

### 109 **STAIR effectively integrates heterogeneous ST data in spatial embeddings**

110 We first quantitatively evaluated STAIR's efficacy in integrating spatial embeddings and identifying  
111 unified spatial domains across diverse tissue sections, a prerequisite for downstream analysis.

112 Effective integration should identify shared signals across specimens while retaining biologically  
113 unique variations within each individual sample.

114 Our initial testing utilized 10X Visium dataset derived from the human dorsolateral prefrontal  
115 cortex (DLPFC)<sup>20</sup>, spanning three samples with four sequential sections per sample. The original  
116 study performed precise manual annotation, delineating white matter (WM) and six gray matter  
117 layers ranging from Layer 1 to Layer 6 to provide ground truth labels (Fig. 2A). First, we conducted  
118 separate spatial domain identification from slices of each sample, which had close locations with  
119 some differences. STAIR achieved the most accurate domain division results on all three samples  
120 (Fig. 2B, Supplementary Fig. S1), with respective median Adjusted Rand Index (ARI) values of  
121 0.60, 0.53, 0.62 (Fig. 2C).

122 Then, we processed twelve slices from three samples simultaneously (Fig. 2D; Supplementary  
123 Fig. S2A). STitch3D was excluded from this test due to its requirement for 3D coordinates to handle  
124 multiple slices, which were not available. Despite the challenge, STAIR maintained the highest  
125 consistency with annotations, achieving a median ARI value of 0.65, far exceeding the second-  
126 ranked STAligner with a median value of 0.46 (Fig. 2C, right). Notably, simultaneous consideration  
127 of three samples proved superior to evaluating each sample individually, resulting in higher ARI  
128 and a clearer demarcation between Layer 4, Layer 5, and Layer 6 (Fig. 2B to D). Subsequently, we  
129 performed low-dimensional visualization using uniform manifold approximation and projection  
130 (UMAP)<sup>21</sup> based on the spatial embeddings derived by these methods (Supplementary Fig. S2B).  
131 In the STAIR-based visualization, all spots exhibited an arrangement according to the layers, with  
132 thorough mixing between the different samples. In contrast, both STAligner and PRECAST lacked  
133 clarity in arranging and distinguishing these known layers. Specifically, STAligner mixed Layer 2  
134 and Layer 3, as well as Layer 4 to Layer 6, while PRECAST only distinguished WM. We also  
135 quantified the effects of spatial embedding learning and integration using Average Silhouette width  
136 (ASW). We calculated ASW for spatial embeddings with respect to spatial domains ( $ASW_{domain}$ )  
137 and samples ( $ASW_{batch}$ ), as well as  $ASW_{F1}$  to evaluate overall capability (Methods). Higher  
138  $ASW_{F1}$  and  $ASW_{domain}$  coupled with lower  $ASW_{batch}$  indicates better performance. STAIR  
139 achieved best spatial embedding learning and integrating with the highest  $ASW_{F1}$  (Supplementary

140 Fig. S2C). STAligner also adequately integrated samples, as indicated by an  $ASW_{batch}$  value  
141 similar to STAIR. However, it had weaker feature learning capabilities with a much lower  
142  $ASW_{domain}$ , which was consistent with the unclear UMAP pattern we observed previously.

143 Moreover, to evaluate cross-platform integration, we applied STAIR to integrate mouse  
144 olfactory bulb data from Stereo-seq<sup>22</sup> and Slide-seqV2<sup>23</sup>, which differed in resolution and area.  
145 Stereo-seq covered the main olfactory bulb (MOB) at sub-single-cell resolution, whereas Slide-  
146 seqV2 encompassed both MOB and the accessory olfactory bulb (AOB) with a resolution of 10  $\mu$ m,  
147 approximating single-cell. STAIR clearly delineated the MOB region common to both datasets and  
148 the AOB region unique to Slide-seqV2 (Fig. 2E, top), highly consistent with standard Allen Brain  
149 Atlas (ABA) partitioning (Supplementary Fig. S2D). The AOB region, situated in the middle and  
150 upper part of the olfactory bulb, comprised two sub-regions: AOBmi and AOBgr. The MOB region  
151 encompassed seven sub-regions arranged in a concentric ring: Rostral migratory stream (RMS),  
152 Granule cell layer (GCL), two Mitral cell layers (MCLs), External plexiform layer (EPL),  
153 Glomerular layer (GL), and Olfactory nerve layer (ONL). In contrast, STAligner struggled to  
154 identify the RMS layer and confused the EPL and GL layers of Stereo-seq (Fig. 2E, middle).  
155 PRECAST failed to identify coherent spatial patterns (Fig. 2E, bottom). UMAP visualization further  
156 showed STAIR effectively distinguished between AOB and MOB in low-dimensional space,  
157 preserving the AOBmi and AOBgr sub-regions in Slide-seqV2 data (Fig. 2F, G). Simultaneously,  
158 STAIR seamlessly integrated the shared MOB region, arranging sub-layers consistent by physical  
159 locations. Conversely, while STAligner achieved integration to a certain extent, it failed to discern  
160 the distinct difference between AOB and MOB. PRECAST completely mixed the datasets, losing  
161 Slide-seqV2 specificity.

162 In summary, STAIR successfully integrated the spatial embeddings across slices within  
163 samples, across samples, and across platforms, ensuring a consistent spatial region division and  
164 preserving unique biological variations.

### 165 **Precise alignment of 2D coordinates across slices by STAIR**

166 A single ST sequencing only acquires data from one slice, resulting in the loss of the unified physical  
167 space across multiple slices. Aligning spatial embeddings across diverse ST slices enables unified

168 molecular feature space that encapsulates spatial information. In this section, we evaluate STAIR's  
169 ability in aligning and integrating ST slices in 2D coordinates (x- and y-axis).

170 We utilized 12 MERFISH slices of the preoptic area of the mouse hypothalamus<sup>2</sup> with known  
171 3D positions. To test the 2D position alignment of slices, we introduced random rotations and  
172 translations to 11 slices while keeping the first slice fixed (Fig. 3A). Subsequently, we employed  
173 STAIR, PASTE, and STitch3D on the rotated slices and assessed their effectiveness (Fig. 3B).  
174 STAIR stood out as the most precise alignment, closely recovering actual coordinates. In contrast,  
175 STitch3D and PASTE struggled with accurate alignment. Quantitatively, the median rotation and  
176 translation errors (Methods) for STAIR were 0.03 and 0.04 mm (Fig. 3C). Similar results were  
177 obtained across 500 random simulations (Supplementary Fig. S3A). In contrast, PASTE exhibited  
178 rotation and translation errors of 1.53 and 1.81, while STitch3D had errors of 2.0 and 2.1,  
179 respectively (Fig. 3C).

180 We further assessed STAIR's robustness on the alignment of 2D coordinates. First, we  
181 examined the impact of resolution by aggregating neighboring cells into virtual lower resolution  
182 spots (Supplementary Fig. S3B). With 2-5 aggregated cells per spot, STAIR maintained low median  
183 rotation errors of 0.02-0.07 and translation errors of 0.04-0.10 (Supplementary Fig. S3C). In contrast,  
184 PASTE had errors between 1.54-1.55 for rotation and 1.78-1.80 for translation, while STitch3D  
185 ranged from 1.23-1.93 and 1.78-2.25, respectively. Additionally, given that fine alignment relied on  
186 spatial region information, we examined performance across 8-15 spatial regions (Supplementary  
187 Fig. S3D). STAIR demonstrated stable alignment, with median rotation errors of 0.02-0.08 and  
188 translation errors of 0.03-0.09.

189 In short, ground truth hypothalamus data confirmed STAIR's capabilities for precise 2D slice  
190 alignment and robustness across varied resolution and spatial domains.

### 191 **Construction of *de novo* 3D atlas by STAIR**

192 Although we aligned spatial embeddings and 2D spatial coordinates, computational construction of  
193 *de novo* 3D atlas with only ST data posed a significant challenge. One of the key difficulties was  
194 computationally determining inter-slice position because the slices used for constructing atlas might  
195 come from varied samples, lacking standardized inter-slice distances. Hence, we aimed to build a



196 3D atlas without prior position knowledge or paired images.

197 First, we tested z-axis coordinate reconstruction on 12 mouse hypothalamic preoptic area slices  
198 generated by MERFISH, where the z-axis location of each slice was known which could serve as a  
199 ground truth<sup>2</sup>. We employed STAIR-Emb (Supplementary Fig. S4A, B) and the inter-slice attention  
200 score derived from STAIR-Emb showed a strong negative correlation with physical distance  
201 (Spearman's  $\rho = -0.88$ , Fig. 4A, B), indicating its potential to reconstructing z-axis. By employing  
202 MST on attention matrix, we achieved accurate z-axis reconstruction, evidenced by the Pearson  
203 correlation coefficient (*PCC*) of 1 and coefficient of determination ( $R^2$ ) of 1 with the ground  
204 truth of z-axis coordinates (Fig. 4C). We further sequentially aligned the x-axis and y-axis of slices  
205 followed by the reconstructed z-axis. This process led to precise *de novo* 3D coordinates (Fig. 4A,  
206 right), showing high consistency with the known 3D coordinates (Fig. 4D). Moreover, we added an  
207 additional 12 slices from another sample of a different gender, and the results showed high accuracy  
208 for the prediction of the total 24 slices by STAIR, with *PCC* and  $R^2$  of 0.99 and 0.94, respectively  
209 (Supplementary Fig. S4C to E).

210 Next, we took a more challenging task using 40 mouse brain slices across three different  
211 samples generated from the ST platform<sup>8</sup>. This dataset covered 40 coronal hemi-brain sections from  
212 the olfactory bulb to the hindbrain. The original study provided anteroposterior (AP)-axis  
213 coordinates based on paired images and Bregma coordinates of the brain<sup>24</sup> (Fig. 4E, left). We started  
214 by using STAIR-Emb to achieve efficient spatial feature integration and spatial region division (Fig.  
215 4F). Despite complexity, a robust correlation between attention scores and physical positions  
216 persisted, with a  $\rho$  of -0.83 (Fig. 4E middle, Supplementary Fig. S5A, left). Further, *PCC* and  $R^2$   
217 between reconstructed AP-axis and the ground truth were as high as 0.98 and 0.96, respectively  
218 (Supplementary Fig. S5A, right). Subsequently, we employed STAIR-Loc to align dorsoventral  
219 (DV)-axis and mediolateral (ML)-axis coordinates based on the slice order of reconstructed AP axis  
220 coordinates, completing the 3D *de novo* construction (Fig. 4E, right; Supplementary Fig. S5B). The  
221 accuracy of spatial positioning of each domain was evident by high expression of their  
222 corresponding marker genes (Fig. 4G). For instance, there was high expression of marker genes *Dsp*  
223 <sup>25</sup>, *Gpr88* <sup>26,27</sup>, *Ramp3* <sup>28,29</sup>, and *Camk2n1* <sup>30</sup> in the hippocampus, striatum, thalamus, and superficial

224 cortex, respectively. To sum up, STAIR enabled accurate *de novo* 3D reconstruction based on ST  
225 slices only.

### 226 **3D modeling of breast tumor microenvironment**

227 To further illustrate biological insights provided by 3D atlas, we analyzed the HER2-positive breast  
228 cancer<sup>31</sup> ST data comprising three consecutive slices (H1 to H3) (Supplementary Fig. S6A). The  
229 pathologists<sup>31</sup> annotated one slice (H1) with six tissue types: invasive cancer, adipose tissue,  
230 connective tissue, breast glands, *in situ* cancer, and immune infiltrates (Fig. 5A).

231 First, STAIR integrated the spatial embeddings of all the three slices, yielding spatial domains  
232 highly consistent with the pathological annotations (Supplementary Fig. S6B). On slice H1, STAIR  
233 achieved an ARI of 0.36, surpassing that of STAligner, STitch3D, and PRECAST, which ranged  
234 from 0.30 to 0.32 (Supplementary Fig. S6C). Recognizing the inherent distinctions between  
235 transcriptome and pathological phenotypes, we deconvoluted<sup>32</sup> each spot with scRNA-seq<sup>33</sup> data to  
236 facilitate spatial domain annotation (Supplementary Fig. S7). STAIR's spatial regions were  
237 annotated as connective tissue, immune cancer, breast glands, adipose tissue, fibrous tissue near the  
238 tumor, invasive cancer, and two *in situ* cancer regions (Fig. 5B). In contrast, STAligner failed to  
239 differentiate the *in situ* cancer area from the invasive cancer area (cluster 0) (Supplementary Fig.  
240 S6B). STitch3D could not distinguish between the two *in situ* cancer areas (cluster 4). PRECAST  
241 struggled to separate the two spatially distinct *in situ* cancer areas (cluster 2, 3, and 5). Additionally,  
242 none of them could detect a heterogeneous region near tumor with fewer cancer cells and more  
243 immune cells (cluster 7).

244 Next, we reconstructed the 3D coordinates. The inferred z-axis distance, at 0.52/0.43, closely  
245 corresponded the true distance ratio. We then aligned the x-axis and y-axis positions in the order of  
246 the z-axis, revealing a continuous structure for each spatial region in the 3D space (Fig. 5C). While  
247 STAligner and STitch3D cannot infer z-axis, we compared STAIR with them in 2D coordinates  
248 alignment (Supplementary Fig. S6D) and employed LISI metric to assess the spatial clustered  
249 pattern of domains in the stacked 2D space, which was a comprehensive measure of spatial domain  
250 identification and 2D coordinates alignment (Supplementary Fig. S6E). STAIR showed best  
251 performance with the lowest median LISI value of 1.53.

252 Furthermore, we examined developmental trajectories<sup>34</sup> and 3D heterogeneity of tumor-  
253 associated domains. To select the initial domain of the developmental trajectory, we conducted a  
254 differential expression analysis of two *in situ* cancer regions (Supplementary Fig. S8A). *In situ*  
255 cancer-1, marked by high expression of the ERBB2<sup>35</sup> gene and S100 family genes<sup>36</sup>, showcased  
256 stronger malignancy and invasive potential. In contrast, *in situ* cancer-2, chosen as the starting  
257 region for trajectory inference, showed a relatively lower malignancy and a higher immune level,  
258 confirmed by overexpressed HLA family<sup>37</sup> genes and enriched immune cells. The trajectory  
259 unveiled a progression from *in situ* cancer-2 to *in situ* cancer-1, invasive cancer, and fibrous tissue  
260 near the tumor (Fig. 5D, Supplementary Fig. S8B), with genes exhibiting expression changes along  
261 the developmental trajectory (Fig. 5E). Notably, within the same area, tumor invasion exhibited  
262 inter-slice heterogeneity on the z-axis. For instance, *in situ* cancer-1 displayed a trend from H3 to  
263 H1, while *in situ* cancer-2 exhibited a trend from H1 and H3 to H2. Invasive cancer also followed a  
264 progression from H3 to H1 (Fig. 5F, Supplementary Fig. S8C).

265 To conclude, STAIR discerned tumor heterogeneity that cannot be identified by the other  
266 methods by integrating three ST slices. The 3D reconstruction of tumor tissue enabled analyzing  
267 heterogeneity of invasion paths in a 3D view.

### 268 **Assimilating new sections into a reference atlas with STAIR**

269 Finally, we tested STAIR's ability to integrate new slices into 3D atlas with molecular feature and  
270 physical coordinates, which enables continuous expansion and update of the existing 3D atlas.

271 We first assessed the ability for predicting the z-axis of new slices by STAIR. By sequentially  
272 masking the known z-axis coordinates of 12 slices in the MERFISH mouse hypothalamic preoptic  
273 dataset, we predicted the masked values based on attention scores. Remarkably, the *PCC* between  
274 predicted and actual coordinates was 0.98, with an  $R^2$  of 0.95. Expanding this analysis to 24 slices  
275 from two hypothalamic preoptic samples, the *PCC* and  $R^2$  still reached 0.98 and 0.94,  
276 respectively. Further testing on 40 ST mouse brain slices resulted in even higher *PCC* and  $R^2$   
277 values of 0.99 and 0.98, respectively (Supplementary Fig. S9). Our analysis showed that STAIR  
278 enabled accurate z-axis prediction, even for slices from multiple samples.

279 Next, we evaluated its capability to integrate new slices into the existing 3D atlas. We

280 integrated a new slice from the Visium platform into an existing 3D ST-platform brain atlas<sup>8</sup>, which  
281 was aligned to Allen Mouse Common Coordinate Framework (CCF)<sup>38</sup> 3D space through  
282 experimental information and image registration. We input 40 ST and the Visium slice into STAIR-  
283 Emb for inter-slice attention scoring (Fig. 6A) and seamlessly mixed spatial embeddings (Fig. 6B).  
284 Leveraging attention scores to predict the position of the new slice (Methods), we identified the  
285 nearest neighbor slice, 20A, in the 3D brain atlas. By taking the 2D coordinates of 20A as a reference  
286 template, STAIR-Loc performed scaling, rotation, and translation on the new Visium slice to map  
287 CCF 3D coordinates (Fig. 6C). Additionally, leveraging detailed spatial anatomical region  
288 annotations from the ABA, we secured regional information for each spot in the Visium slice (Fig.  
289 6D). The UMAP-based visualization revealed internal clustering of anatomical regions and  
290 separation between regions (Fig. 6E). We further demonstrated the accuracy of regional annotation  
291 of the new Visium slice based on the expression of specific markers, such as *Cabp7*, *Hpcal1*, *Gpr88*,  
292 *Rora*, *Mbp* and *Pmch*, which exhibited high expression in hippocampus, hippocampal formation,  
293 striatum, thalamus, fiber tracts and hypothalamus, respectively.

294 To summarize, STAIR enabled integrating new slices into a 3D atlas which might be generated  
295 from a different ST platform.

296

## 297 **Discussion**

298 The rapid advances in ST have ushered in new opportunities for exploring tissue architecture with  
299 gene expression patterns. However, connecting perspectives across discrete 2D slices to enable  
300 unambiguous 3D biological comprehension presented persistent computational challenges. Here,  
301 we provide an integrated solution for robust alignment, construction to 3D modelling, and  
302 assimilation of emerging data.

303 STAIR achieves accurate spatial embedding and coordinate alignment, enabling pioneering *de*  
304 *novo* 3D atlas construction from ST slices only. Its superior efficacy and broad functionality are  
305 attributed to the attention mechanism of the heterogeneous graph attention network. First, it enables  
306 adaptive feature aggregation by capturing spot-level and slice-level relationships, thereby obtaining  
307 spatial embeddings informed by broader context. These embeddings further enable slice anchor

308 pairs to initialize 2D alignments. Second, the attention mechanism is highly interpretable and  
309 versatile. High-order semantic modeling captures the physical relationships between slices and  
310 provides an innovative z-axis positioning mechanism, which facilitates multi-sample 3D  
311 reconstruction and seamless assimilation of new slices.

312 While most of the previous ST aligners focus on 2D alignment or integration, STAIR and  
313 STitch3D take multiple parallel ST slices as input and aim to create integrated 3D spatial atlases.  
314 However, STAIR is technically distinguished from STitch3D in several aspects. (1) Input flexibility:  
315 STAIR requires only ST data as input, making it more readily applicable to datasets where matched  
316 single-cell data is not available. (2) *De novo* 3D reconstruction: STAIR can infer relative positioning  
317 of slices along the z-axis in a completely unsupervised manner. This enables fully data-driven 3D  
318 reconstruction without relying on known slice spacing or order information. (3) New slice  
319 assimilation: STAIR can predict the positioning of new slices based on attention score proximities  
320 and situate them within existing 3D atlases by transferring coordinate templates. This unique  
321 capability paves the way for continually expanding spatial references. (4) Coordinate alignment:  
322 While STitch3D aligns spots by 3D coordinate registration, STAIR offers an alternative approach  
323 using sequential 2D alignment between slice pairs guided by learned spatial embeddings. This  
324 provides greater flexibility when 3D location inputs are unreliable or unavailable.

325 Despite progress, further innovation must meet escalating biological complexity and spatial  
326 dimension. First, one current limitation is the effective integration of datasets from platforms with  
327 highly divergent resolutions, such as attempting to jointly analyze Stereo-seq data that profiles  
328 transcriptomes at subcellular resolution with ST data that assays much larger tissue spots. Second,  
329 integration of ST datasets with other data types such as spatial proteome will be a significant  
330 challenge. At application horizon, advancing analytical tools based on 3D atlas are needed. For  
331 example, most current spatially variable gene identification primarily models in 2D space, whereas  
332 capturing full organ system patterns in 3D could provide deeper biological insights.

333 In conclusion, STAIR provides a unified algorithm advancing analysis of multi-slice ST data,  
334 including alignment, integration, and *de novo* 3D reconstruction. This advancement facilitates the  
335 creation of spatial maps for diverse organs, enabling the exploration of molecular mechanisms

336 underlying tissue structure phenotypes in a true 3D dimension.

337

### 338 **STAIR algorithm**

339 **Data preprocessing.** Suppose that there are  $S$  slices denoted as  $A_1, A_2, \dots, A_S$ , each containing  
340 respective numbers of spots  $N_1, N_2, \dots, N_S$ . Among these slices,  $G$  genes are common.  
341 Consequently, the gene expression data can be represented as a matrix  $X$  of dimensions  $N \times G$ ,  
342 where  $N = N_1 + N_2 + \dots + N_S$  is the total number of spots across all slices. The spatial coordinate  
343 data is stored in a matrix  $Y$  of dimensions  $N \times 2$  or  $N \times 3$  depending on if the z-dimension  
344 exists, and it is sufficient to input an  $N \times 2$  dimensional coordinate matrix for STAIR. The raw  
345 gene expression counts in  $X$  are normalized based on library size and then log-transformed to get  
346 the normalized expression matrix  $\tilde{X}$ .

347 To remove batch effects in expression features across various slices, we employed an  
348 autoencoder alongside batch annotation<sup>16</sup>  $b_{ns}$ . If the  $n$ th spot is from the  $s$ th slice, we set  $b_{ns} =$   
349 1; otherwise, we set  $b_{ns} = 0$ . Given the assumptions of negative binomial (NB) or zero-inflated  
350 negative binomial (ZINB) distributions in gene expression, the preprocessing framework is:

$$351 \quad Z = f_1(\tilde{X}||B)$$

$$352 \quad Z' = f_2(Z||B)$$

$$353 \quad R = f_3(Z')$$

$$354 \quad \Pi = f_4(Z')$$

355 Encoder  $f_1$  contains two layers compressing the expression matrix into a 32-dimensional low-  
356 dimensional feature matrix  $Z$ . The decoder first uses  $f_2$  to decode  $Z$  and batch information into  
357 a 128-dimensional feature matrix  $Z'$ , the parameters of NB distribution ( $R, L$ ) and zero-inflated  
358 probability  $\Pi$  are then learned based on  $Z'$ . The objective is to minimize reconstruction loss  
359 between  $X$  and the NB/ZINB distribution parameterized by  $(\Pi, R, P)$ . The loss function is the  
360 NB/ZINB negative log-likelihood.

361

362 **Spatial embedding alignment.** We use a heterogeneous graph attention network<sup>15</sup> to learn  
363 integrated spatial features across slices.

364

365 Construction of heterogeneous graph. We attribute node characteristics to each spot based on the  
366 slice it belongs to. Distinct approaches are employed to establish edges for spots located within the  
367 same slice and those positioned across different slices.

368 For spots in the same slice, we build homogeneous edges based on the physical location of the  
369 spot. For a spot with index  $j$  in slice  $A_j$ , the set of its intra-slice neighbors  $\mathcal{N}_j$  is identified by K-  
370 Nearest Neighbor (KNN) based on spatial coordinates.

371 For spots not within the same slice, since their relative physical coordinates are unknown, we  
372 construct heterogeneous edges based on the expression similarity obtained in the preprocessing step.  
373 Only nodes with highly consistent expression features are connected. For spots  $j$  from slice  $A_j$   
374 and  $k$  from slice  $A_k$ , the edge exists if  $z_k \cdot z_j > t$ . We usually set  $t = 0.9$  and denote the inter-  
375 slice neighbors of spot  $j$  from slice  $A_k$  as  $\mathcal{N}_j^{JK}$ .

376

377 Intra-slice information aggregation. To learn the spatial features of each spot, we first aggregate the  
378 information from intra-slice neighbors based on homogeneous edges separately for each slice.

379 We adopted the same model architecture and aggregation method as the graph attention network  
380 (GAT) module in SECE<sup>39</sup>, and obtained the homogeneous spatial feature  $U^{hom}$  based on  
381 homogeneous edges,

$$382 \quad U^{hom} = \text{GAT}(Z, Y)$$

383 where  $Z$  is the expression feature of the spot obtained by the preprocessing module.

384

385 Inter-slice information aggregation. Further, we employ spot and slice level attention to aggregate  
386 inter-slice information adaptively.

387 First, we learn spot-level attention. For two spots  $i$  and  $j$  from slices  $A_i$  and  $A_j$  connected  
388 by heterogeneous edge, the spot-level attention  $e_{ij}^{IJ}$  between them represents the importance of spot  
389  $j$  to  $i$ , namely,

$$390 \quad e_{ij}^{IJ} = \text{LeakyReLU}(q_{IJ}^T [W_{IJ}^1 u_i^{hom} || W_{IJ}^2 u_j^{hom}])$$

391 where  $W_{IJ}^1$  and  $W_{IJ}^2$  are weight matrices specific to slice pairs,  $q_{IJ}$  is a learnable vector, and  $e_{ij}^{IJ}$

392 is an asymmetric attention matrix that contains pairwise attention between slices  $A_I$  and  $A_J$ . The  
 393 final inter-slice spot level attention matrix  $\alpha_{ij}^{IJ}$  is obtained by normalizing  $e_{ij}^{IJ}$ :

$$394 \quad \alpha_{ij}^{IJ} = \text{softmax}_j(e_{ij}^{IJ}) = \frac{\exp(e_{ij}^{IJ})}{\sum_{k \in \mathcal{N}_i^{IJ}} \exp(e_{ik}^{IJ})}.$$

395 For a node  $i$  from slice  $A_I$ , its spot-level heterogeneity based on neighbors in slice  $A_J$  is:

$$396 \quad u_i^{IJ} = \sigma \left( \sum_{j \in \mathcal{N}_i^{IJ}} \alpha_{ij}^{IJ} \cdot u_j^{hom} \right).$$

397 Then, we learn slice-level attention. Different slices contribute differently to target slice and  
 398 we adaptively learn how much each slice contributes to others. For the slice  $A_I$  to be learned, the  
 399 slice-level importance of slice  $A_J$  to  $A_I$  is:

$$400 \quad w_{IJ} = \frac{1}{N_I} \sum_{i \in A_I} q^T \cdot \tanh(W \cdot u_i^{IJ} + b),$$

401 where  $W$  and  $b$  are weight matrix and bias vector,  $q$  is a learnable vector. Then normalize  $w_{IJ}$   
 402 to get the final slice level attention coefficient:

$$403 \quad \beta_{IJ} = \frac{\exp(w_{IJ})}{\sum_{K \neq I} \exp(w_{IK})}.$$

404 Therefore, the heterogeneity representation of slice  $A_I$  based on other slices is:

$$405 \quad U_I^{het} = \sum_{J \neq I} \beta_{IJ} U^{IJ}.$$

406

407 Model learning and training. For each slice, the final spatial feature matrix  $U$  is obtained by  
 408 combining the intra-slice representation  $U^{hom}$  and inter-slice heterogeneous representation  $U^{het}$ :

$$409 \quad U = \lambda \cdot U^{hom} + (1 - \lambda) \cdot U^{het}$$

410 where  $\lambda$  weights the homogeneous and heterogeneous components with default value 0.8. The  
 411 model is trained to ensure  $U$  reliably represents the original spatial gene expression features  $Z$ .

412 The objective function is defined as the mean squared error between  $U$  and  $Z$ :

$$413 \quad Loss = MSE(U, Z)$$

414 In the training process,  $U$  is set to 32 dimensions. The Adam optimizer is used for training  
 415 with learning rate of 0.001. The default number of iterations is 150.

416

417 **Slice-level attention-based reconstruction and prediction in z-axis.** The attention weight at the



418 slice level, denoted as  $\beta_{IJ}$ , characterizes the collective impact of slice  $A_J$  on  $A_I$  within the spatial  
 419 embedding learning process. This encapsulates intricate higher-order spatial semantic insights.  
 420 Notably, the strong correlation between these weights and the actual distance between slices  
 421 signifies the potential for deducing the physical placement of slices.

422

423 De novo z-axis reconstruction for multiple slices. When we lack information about the third-  
 424 dimensional coordinates  $(y_1^{(3)}, \dots, y_I^{(3)}, \dots, y_S^{(3)})$  of the slice, we can infer the positional  
 425 relationships between these parallel slices based on the inter-slice attention scores. Specifically, we  
 426 start by defining the distances between slices  $A_J$  and  $A_I$  as  $d_{IJ} = 1 - \frac{\beta_{IJ} + \beta_{JI}}{2}$  and proceed to  
 427 construct a Kruskal algorithm<sup>19</sup> based MST using *network* package implemented in Python.  
 428 Subsequently, we select the given root slice  $A_I$  and set its position as  $l_I = 0$ . The positions of the  
 429 remaining nodes are then determined by adding the distance between each node and its parent node's  
 430 position. Lastly, we normalize the distances to obtain position predictions  $(l_1, l_2, \dots, l_S)$  within the  
 431 range of 0 to 1. Furthermore, for comparison with actual coordinates in the article, we additionally  
 432 scale the normalized distances  $(l_1, l_2, \dots, l_S)$  to match the real coordinate range.

433

434 Z-axis prediction for new slice. When the z-axis coordinates  $(y_1^{(3)}, y_2^{(3)}, \dots, y_S^{(3)})$  are known, in  
 435 order to align the new slice  $A_{new}$  into the unified 3D space, we predict  $y_{new}^{(3)}$  based on the  
 436 attention vectors between  $A_{new}$  and  $A_1, A_2, \dots, A_S$ , denoted as  $\beta_1 = (\beta_{new,1}, \beta_{new,2}, \dots, \beta_{new,S})$   
 437 and  $\beta_2 = (\beta_{1,new}, \beta_{2,new}, \dots, \beta_{S,new})$ .

438 We first sort the elements of  $\beta_1$  and  $\beta_2$  in descending order, and choose the top  $N$  elements  
 439  $\hat{\beta}^1 = (\hat{\beta}_{new,R_1^1}, \dots, \hat{\beta}_{new,R_N^1})$  and  $\hat{\beta}^2 = (\hat{\beta}_{new,R_1^2}, \dots, \hat{\beta}_{new,R_N^2})$ . Following this, we identify the  
 440 intersection of these element indices  $\{R_1, \dots, R_{N'}\}$ , where  $N' \leq N$ . Finally, we perform weighted  
 441 average on the z-axis corresponding to  $(R_1, \dots, R_{N'})$  to get the predicted value of  $y_{new}^{(3)}$ :

$$442 \quad \hat{y}_{new}^{(3)} = \frac{\sum_{K \in \{R_1, \dots, R_{N'}\}} \frac{\beta_{new,K} + \beta_{K,new}}{2} \cdot y_K^{(3)}}{\sum_{K \in \{R_1, \dots, R_{N'}\}} \frac{\beta_{new,K} + \beta_{K,new}}{2}} \quad (1)$$

443

444 **Spatial location alignment.** We employ a two-stage approach for 2D alignment in x-axis and y-

445 axis. In the initial stage, spatial features are utilized to identify spot pairs with precise matches, and  
446 initial transformation matrices are determined based on these pairs. In fine alignment stage, we first  
447 identify spots that effectively capture both global and local information within slices. The coordinate  
448 positions of these spots are then leveraged to execute ICP<sup>18</sup> fine registration.

449

450 Initial alignment. Consider slice  $A_I$  with  $n_I$  spots and slice  $A_J$  with  $n_J$  spots, along with their  
451 spatial feature sets  $\{u_1^I, u_2^I, \dots, u_{n_I}^I\}$  and  $\{u_1^J, u_2^J, \dots, u_{n_J}^J\}$ , respectively. First, we measure the  
452 similarity between spots through the cosine distance based on spatial embeddings. The mutual  
453 nearest neighbors (MNN) of  $k = 1$  located in different slices form pairs for the initial alignment,  
454 resulting in curated pairs  $\{(i_1, j_1), (i_2, j_2), \dots, (i_n, j_n)\}$  along with their coordinates  
455  $\{(y_{i_1}^I, y_{j_1}^J), (y_{i_2}^I, y_{j_2}^J), \dots, (y_{i_n}^I, y_{j_n}^J)\}$ . subsequently, we seek the optimal rotation matrix  $R$  and  
456 translation vector  $t$ , to align the physical positions of the corresponding point sets. Consequently,  
457 the loss function for the initial alignment is formulated as:

$$458 \quad Loss_{init} = \sum_{k=1}^n |y_{i_k}^I - (Ry_{j_k}^J + t)|^2$$

459 Singular value decomposition<sup>40</sup> solves for  $R$  and  $t$ . All spots are aligned to their targets  
460 accordingly.

461

462 Fine alignment. The fine alignment stage involves two main steps: identifying informative anchor  
463 spots for capturing both regional details and global outlines specific to the slice, followed by the  
464 application of the classic ICP<sup>18</sup> algorithm. First, we select highly concentrated regions that are  
465 common to both slices, according to median of LISI value which implemented in R package *lisi*.  
466 Subsequently, we identify the concave hulls<sup>41</sup> corresponding to the chosen regions and the slices.  
467 These concave hulls serve to depict both the local attributes of the region and the broader shape  
468 characteristics of the entire slice. Finally, ICP<sup>18</sup> algorithm is employed on these sets of informative  
469 points to achieve precise fine registration, resulting in our desired alignment outcome.

470

471 **Aligning new brain slices into existing ABA atlases.** We employed a dataset consisting of 40 ST

472 coronal brain slices with CCF 3D coordinate information, derived from a previous study<sup>8</sup>, to serve  
473 as a foundational reference of whole-brain framework. To obtain the CCF 3D coordinates and  
474 anatomical region annotations of each spot in new slice, we incorporated it into the reference dataset  
475 through the following steps.

476 First, we integrate the spatial embeddings of the new slice  $A_{new}$  with the reference set  $\{A_1, A_2,$   
477  $\dots, A_{40}\}$ , obtaining the attention score associated with the  $A_{new}$  and each reference slice. By  
478 applying formula (1), we predict the AP coordinate of the new slice, denoted as  $y_{AP}^{new}$ .

479 Then, we adjusted the ML and DV dimensions of  $A_{new}$  to align with the CCF scale. We select  
480 the reference slice  $A_j$  closest to  $A_{new}$  according to  $y_{AP}^{new}$ , followed by filtering MNN spot pairs  
481 based on cosine distances between spatial features. This filtering process generated a set of spot  
482 pairs  $\{(i_1, j_1), (i_2, j_2), \dots, (i_n, j_n)\}$ , each possessing corresponding ML and DV coordinates  
483  $\{(y_{i_1}^{new}, y_{j_1}^j), (y_{i_2}^{new}, y_{j_2}^j), \dots, (y_{i_n}^{new}, y_{j_n}^j)\}$ . Consequently, the scaling factor was calculated as:

$$484 \quad scale = Median_{k_1 \neq k_2} \left\{ \frac{|y_{j_{k_1}}^j - y_{j_{k_2}}^j|}{|y_{i_{k_1}}^{new} - y_{i_{k_2}}^{new}|} \right\}.$$

485 Next, the ML and DV orientations of slice  $A_{new}$  are aligned into the CCF. We perform a two-  
486 stage alignment of the scaled coordinates (see **Spatial location alignment**), thus effectively  
487 integrating the 3D coordinates of  $A_{new}$  into the CCF.

488 Finally, anatomical regions are assigned to each new spot based on location-specific  
489 information within the ABA annotation file *annotation\_25.nrrd* from <https://portal.brain-map.org/>,  
490 establishing a mapping of the anatomical context for slice  $A_{new}$ .

491

## 492 **Toolkit for ST analysis**

493 **Clustering for spatial domains.** Clustering is conducted on integrated spatial embeddings to obtain  
494 unified spatial domains across ST slices. We employ mClust<sup>42</sup> clustering method implemented in  
495 R package *rmclust*.

496

497 **Spatial trajectory inference.** Trajectory inference based on spatial embeddings is used to track the

498 development in spatial dimension. We utilize Monocle3<sup>34</sup> to perform the pseudo time inference for  
499 each spot based on UMAP derived from spatial embedding of STAIR by applying *learn\_graph* and  
500 *order\_cells* in Monocle3 package. Function *graph\_test* is employed to find genes that change with  
501 pseudo time.

502

503 **Deconvolution.** For HER2+ breast cancer dataset, we perform deconvolution to analyze the cell  
504 type composition using software Cell2location<sup>32</sup> and annotated scRNA-seq dataset<sup>33</sup>. Cell2location  
505 is run according to the tutorial and default parameters.

506

507 **Differential expression analysis.** We employ Seurat V4<sup>43</sup> to perform differential expression  
508 analysis. Differential expression analysis is used to identify cluster-specific marker genes where all  
509 the clusters are pairwise compared using the Wilcoxon method. Each identified marker gene was  
510 expressed in a minimum of 25% of cells and at a minimum log fold change threshold of 0.25.

511

## 512 **Evaluation**

513 **Evaluation of spatial embedding alignment.** Adjusted Rand index (ARI). ARI measures the  
514 consistency between spatial domains identified by different algorithms and the known anatomical  
515 region labels. Given the contingency table of intersections between the algorithm-generated  
516 domains and annotation-based labels, it is calculated as

$$517 \quad ARI = \frac{\sum_{ij} \binom{n_{ij}}{2} - [\sum_i \binom{a_i}{2} \sum_j \binom{b_j}{2}] / \binom{n}{2}}{\frac{1}{2} [\sum_i \binom{a_i}{2} + \sum_j \binom{b_j}{2}] - [\sum_i \binom{a_i}{2} \sum_j \binom{b_j}{2}] / \binom{n}{2}},$$

518 where  $n_{ij}$ ,  $a_i$  and  $b_i$  are values from the contingency table. ARI values range from -1 to 1. Higher  
519 ARI indicates greater agreement with the ground truth annotations.

520

521 Average Silhouette width (ASW). ASW evaluates how well the features match true clusters in the  
522 data. For every sample  $i$ , Silhouette width  $S(i)$  is calculated as

$$523 \quad S(i) = \frac{b(i) - a(i)}{\max \{a(i), b(i)\}}$$

524 where  $a(i)$  is the average distance between  $i$  and points in its own cluster, and  $b(i)$  is that to  
 525 adjacent cluster points. ASW values range from -1 to 1, with greater ASW indicates better match.

526 In this paper, we employ  $ASW_{domain}$  and  $ASW_{batch}$  to measure the fitness of spatial features  
 527 to known spatial regions and batches of slices, respectively. A larger  $ASW_{domain}$  and a smaller  
 528  $ASW_{batch}$  value represent stronger feature learning and data integration capabilities. To evaluate  
 529 the comprehensive performance of spatial features, we calculated the harmonic mean  $ASW_{F1}$  of  
 530  $ASW_{domain}$  and  $1 - ASW_{batch}$ :

$$531 \quad ASW_{F1} = \frac{2(1 - ASW_{batch})ASW_{domain}}{1 - ASW_{batch} + ASW_{domain}}$$

532 Higher  $ASW_{F1}$  indicates stronger comprehensive ability of feature integration and biological  
 533 specificity retention.

534

535 **Evaluation of spatial alignment in x-axis and y-axis.** To assess STAIR's capability for spatial  
 536 alignment, we conducted simulations involving multiple slices, each with known 3D coordinates.  
 537 Specifically, we maintained the spatial location of the first slice unchanged, while applying random  
 538 rotations and translations to the remaining slices. Rotation angle  $\theta \in (0, \pi)$ , translation distance  
 539  $t_{(1)} \in (-a_{(1)}, a_{(1)})$ ,  $t_{(2)} \in (-a_{(2)}, a_{(2)})$ , where  $a_{(1)} = \max(y_{(1)}) - \min(y_{(1)})$ ,  $a_{(2)} =$   
 540  $\max(y_{(2)}) - \min(y_{(2)})$ . Note that the ground truth rotation angle and translation distance of  $S - 1$   
 541 slices are  $\{\theta^2, \theta^3, \dots, \theta^S\}$  and  $\{(t_{(1)}^2, t_{(2)}^2), (t_{(1)}^3, t_{(2)}^3), \dots, (t_{(1)}^S, t_{(2)}^S)\}$ , respectively. The error of  
 542 rotation and translation are:

$$543 \quad \Delta_{\theta} = \frac{1}{S-1} \sum_{l=2}^S |\theta^l - \hat{\theta}^l|$$

$$544 \quad \Delta_t = \frac{1}{S-1} \sum_{l=2}^S \sqrt{(t_{(1)}^l - \hat{t}_{(1)}^l)^2 + (t_{(2)}^l - \hat{t}_{(2)}^l)^2}$$

545 where  $\hat{\theta}^l$  and  $(\hat{t}_{(1)}^l, \hat{t}_{(2)}^l)$  are rotation angle and translation distance of slice  $A_l$  obtained by the  
 546 algorithm to be evaluated, respectively.

547

548 **Evaluation of spatial domain identification and 2D coordinate alignment in HER2+ breast**  
 549 **cancer.** Local inverse Simpson's index (LISI) measures the degree of local mixing, and we use it to

550 evaluate the spatial aggregation pattern of domains in stacked 2D space. For each spot  $i$ , LISI is  
 551 formulated as:

$$552 \quad LISI(i) = \frac{1}{\sum_{l \in L} p_i(l)},$$

553 where  $p_i(l)$  is the probability that the spatial domain label  $l$  exists in the local neighborhood of  
 554 sample  $i$ , and  $L$  is the set of spatial domains. Local neighborhoods are selected by stacked 2D  
 555 coordinates. The value of LISI is in the range of  $[1, \infty)$ , and smaller LISI indicates better  
 556 aggregation pattern.

557

558 **Evaluation of z-axis reconstruction and prediction.** We utilize the coefficient of determination  
 559 ( $R^2$ ) and the Pearson correlation coefficient ( $PCC$ ) to quantify the effectiveness of z-axis  
 560 reconstruction and prediction. Denoting the ground truth z-axis coordinate of the  $S$  slices as  
 561  $\{y_{(3)}^1, y_{(3)}^2, \dots, y_{(3)}^S\}$ , and the reconstructed or predicted outcomes are  $\{\hat{y}_{(3)}^1, \hat{y}_{(3)}^2, \dots, \hat{y}_{(3)}^S\}$ . The  
 562 corresponding  $R^2$  and  $PCC$  values are calculated as:

$$563 \quad R^2 = 1 - \frac{\sum_{l=1}^S (y_{(3)}^l - \hat{y}_{(3)}^l)^2}{\sum_{l=1}^S (y_{(3)}^l - \bar{y}_{(3)})^2}$$

$$564 \quad PCC = \frac{\sum_{l=1}^S (y_{(3)}^l - \bar{y}_{(3)}) (\hat{y}_{(3)}^l - \bar{\hat{y}}_{(3)})}{\sqrt{\sum_{l=1}^S (y_{(3)}^l - \bar{y}_{(3)})^2} \sqrt{\sum_{l=1}^S (\hat{y}_{(3)}^l - \bar{\hat{y}}_{(3)})^2}}$$

565 where  $\bar{y}_{(3)} = \sum_{l=1}^S y_{(3)}^l$  and  $\bar{\hat{y}}_{(3)} = \sum_{l=1}^S \hat{y}_{(3)}^l$ .

566

567 **Assessment of alternative methods.** We conducted a comparative evaluation of STAIR against  
 568 other alignment methods, including STAligner, Stitch3D, PRECAST, GraphST, and PASTE. In our  
 569 assessment, we employed the default parameters for all methods unless specific parameters were  
 570 outlined in the original text or tutorial.

571

572 STAligner. STAligner integrates ST data across different conditions, technologies, and devel  
 573 opmental stages. It employs STAGATE and triplet loss to integrate the ST datasets until b  
 574 atch-corrected embeddings are generated. It further considers shared spatial domain and M  
 575 NNs identified by STAligner as corresponding pairs to guide the 2D alignment. We downl

576 oaded the package from <https://github.com/zhoux85/STAligner>, and ran STAligner following  
577 its tutorial <https://staligner.readthedocs.io/en/latest/index.html>.

578

579 *STitch3D*. STitch3D first unified 3D spatial coordinates for spots using ICP or PASTE, followed by  
580 graph construction based on 3D coordinates. It performed spatial embedding learning and  
581 integration by graph attention network and slice- and gene-specific parameters. We downloaded the  
582 package from <https://github.com/YangLabHKUST/STitch3D>, and ran STitch3D following  
583 <https://stitch3d-tutorial.readthedocs.io/en/latest/tutorials/index.html>. Given the requirement for  
584 scRNA-seq datasets from the same tissue, we utilized single cell DLPC and HER2+ breast cancer  
585 data accessed at the Gene Expression Omnibus (GEO) under the accession code GSE144136 and  
586 GSE176078, respectively.

587

588 *PRECAST*. PRECAST is a probabilistic method for spatial embedding learning, clustering, and  
589 alignment. We downloaded the R package from <https://github.com/feiyong/PRECAST/>, and ran  
590 PRECAST following its tutorial <https://feiyong.github.io/PRECAST/index.html>

591

592 *PASTE*. PASTE provides the flexibility to align two slices either through pairwise alignment or to  
593 simultaneously align multiple slices using center alignment. We opted for pairwise alignment in our  
594 testing, as other approaches also employ pairwise processes. In pairwise slice alignment, it aims to  
595 find the best possible way to connect spots in one slice with spots in another slice, followed by  
596 constructing a stacked 3D alignment of a tissue. The connection, denoted as  $\Pi$ , is chosen to reduce  
597 both the differences in gene expression patterns between connected spots from different slices and  
598 the differences in physical distances between connected spots within the same slice. Parameter  $\alpha$   
599 was used to balance these two differences, and we set its default value of  $\alpha = 0.1$  in our test. We  
600 download the package from <https://github.com/raphael-group/paste/tree/main>, and ran PASTE  
601 following <https://github.com/raphael-group/paste/tree/main/docs/source/notebooks>.

602

## 603 **Data availability**

604 Visium DLPPFC dataset can be accessed from the spatialLIBD package <http://spatial.libd.org/spatialLIBD>. Olfactory bulb dataset sequenced by Stereo-seq is available at [https://github.com/JinmiaoChenLab/SEDR\\_analyses](https://github.com/JinmiaoChenLab/SEDR_analyses). Olfactory bulb dataset sequenced by Slide-seqV2 is the Puck\_200127\_15 data in <https://singlecell.broadinstitute.org/>. MERFISH hypothalamic preoptic region data is downloaded from [https://github.com/ZhuangLab/MERFISH\\_analysis](https://github.com/ZhuangLab/MERFISH_analysis). Dataset of ST brain slices is available at <http://molecularatlas.org/>, and the Visium brain data aligned to them is downloaded from <https://www.10xgenomics.com/resources/datasets/mouse-brain-coronal-section-1-ffpe-2-standard>. HER2+ breast cancer ST dataset is available at <https://doi.org/10.5281/zenodo.4751624>, and single cell data is accessed at GEO under the accession code GSE176078.

614

## 615 **Code availability**

616 The STAIR algorithm is implemented and provided as a pip installable Python package which is available on GitHub <https://github.com/yuyuanyuana/STAIR>. All scripts used to reproduce all the analyses are also available at the same website.

619

## 620 **Declarations**

### 621 **Ethics approval and consent to participate**

622 No ethical approval was required for this study.

### 623 **Consent for publication**

624 Not applicable.

### 625 **Competing interests**

626 The authors declare that they have no competing interests.



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630 **Authors' contributions**

631 Z.X. conceived and supervised the study. YY.Y. and Z.X. designed the study. YY.Y. analyzed the  
632 data. YY.Y. and Z.X. wrote the manuscript. All authors read and approved the manuscript.

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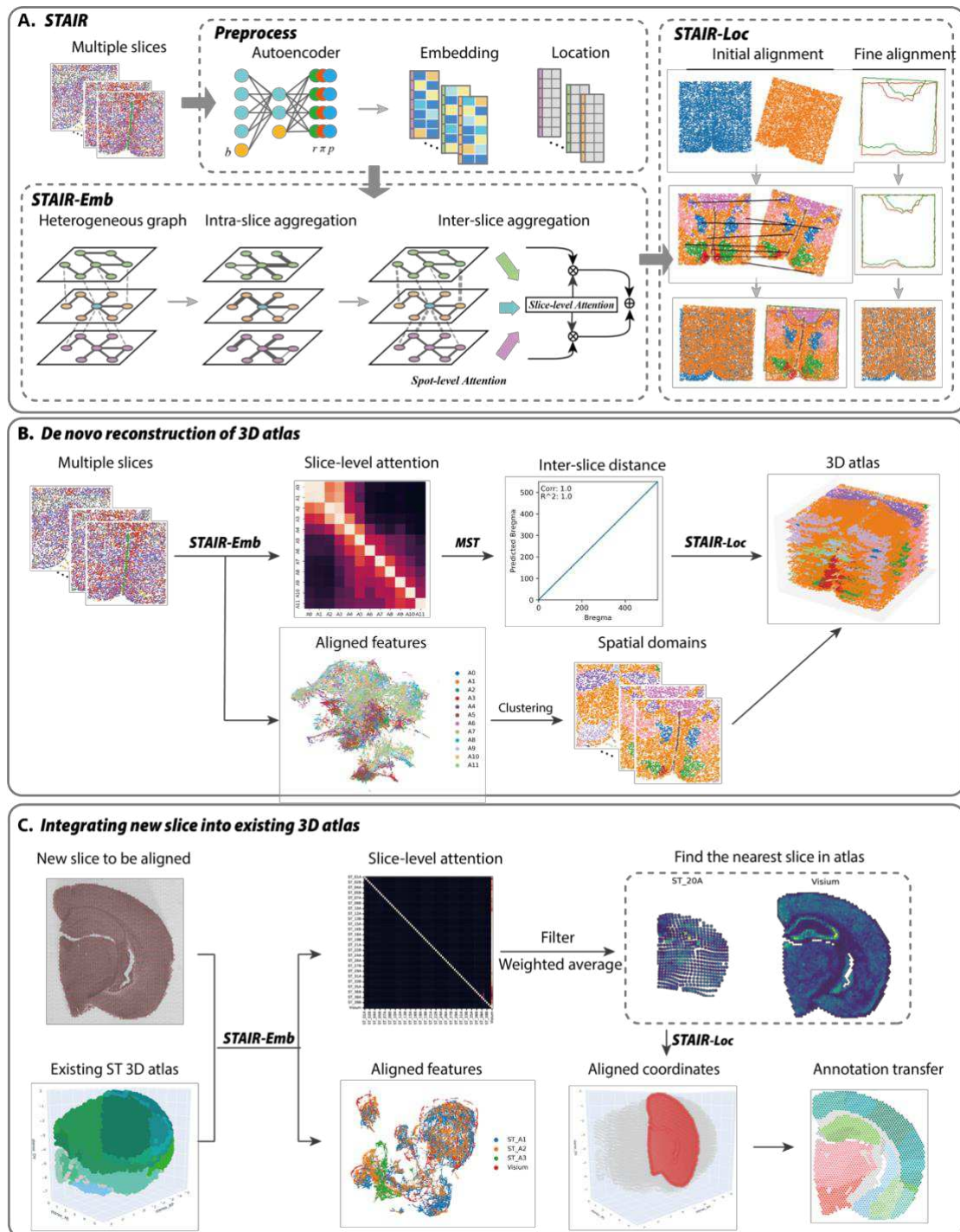
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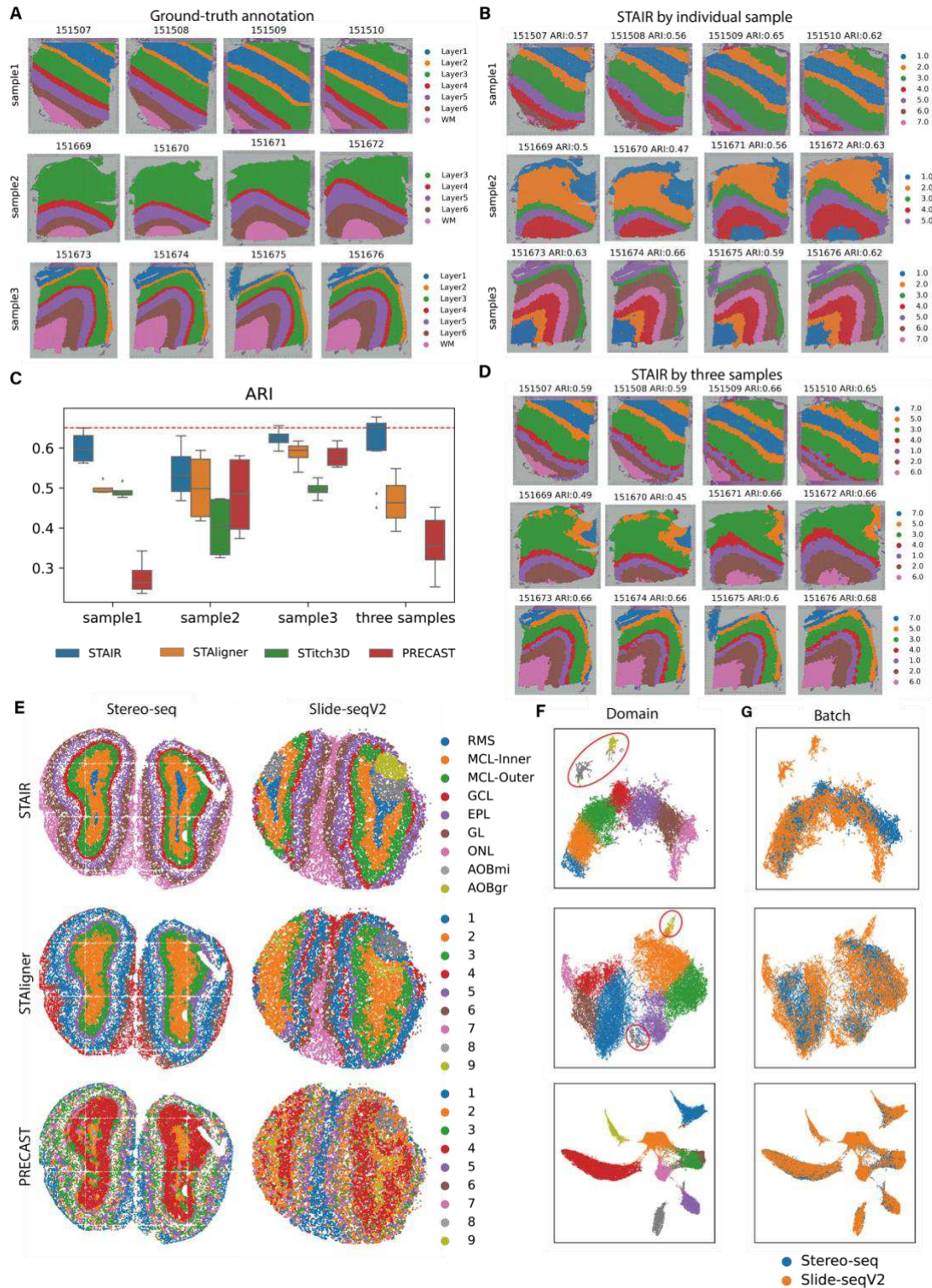
641



650 coordinates, followed by refining the alignment further by incorporating boundary points of slices  
651 and their respective domains. **(B)** *De novo* reconstruction of 3D atlas without prior knowledge about  
652 physical location. STAIR-Emb learns integrated spatial features and establishes high-order semantic  
653 relationships between slices, transforming them into distance matrices. Next, minimum spanning  
654 trees (MST) reconstruct relative positional relationships, guiding sequential spatial alignment. **(C)**  
655 Seamlessly integrating new slices into an existing 3D atlas. STAIR-Emb integrates spatial features  
656 of the new slice with the 3D atlas, followed by predicting the new slice's z-axis location and aligning  
657 its 2D coordinates (x- and y-axis) with the 3D atlas using STAIR-Loc.

658

659



660

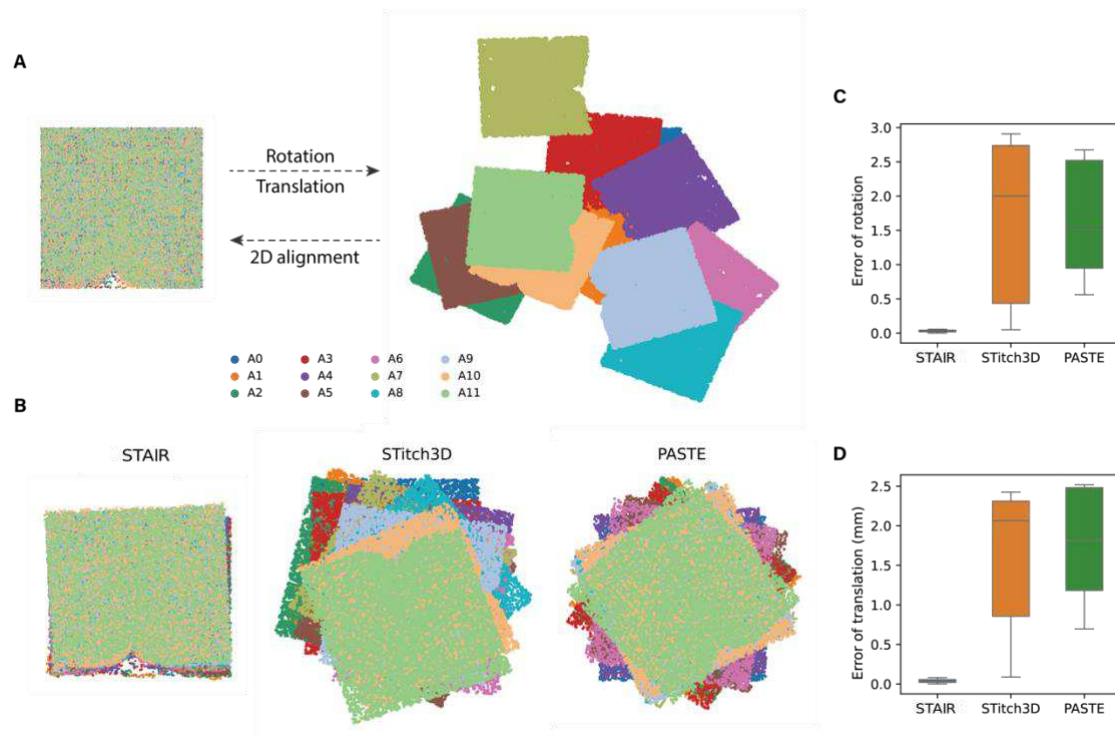
661 **Fig. 2. STAIR effectively integrates heterogeneous spatial transcriptomics data.** (A) Ground-

662 truth segmentation of manually annotated regions in 12 DLPFC sections. (B) STAIR's spatial

663 domain identification based on the 4 DLPFC slices for each sample. (C) Boxplots of adjusted rand

664 index (ARI) scores of the four methods applied to the 4 DLPFC slices of each sample and to the

665 total 12 slices of the three samples. In the boxplot, the center line denotes the median, box limits  
666 denote the upper and lower quartiles, and whiskers denote the  $1.5 \times$  interquartile range. **(D)** STAIR's  
667 spatial domain identification based on the 12 DLPFC slices. **(E)** Integrative spatial regions  
668 identification of Stereo-seq (left) and Slide-seqV2 (right) mouse olfactory bulb data using STAIR,  
669 STAligner and PRECAST. **(F)** UMAPs derived from spatial embedding of STAIR, STAligner and  
670 PRECAST, with colors determined by the spatial regions they identify. **(G)** UMAPs derived from  
671 spatial embedding of STAIR, STAligner and PRECAST, with colors determined by the dataset to  
672 which the spot belongs.  
673



675

676

**Fig. 3. Precise alignment of 2D coordinates by STAIR.** (A) Schematic diagram of spatial position

677

alignment. 2D coordinates in the first slice were fixed, and the remaining 11 slices were randomly

678

rotated and translated. STAIR, PASTE, and STitch3D were employed to align the spatial

679

coordinates of the rotated data. (B) Results of 2D spatial alignment using STAIR, STitch3D and

680

PASTE. (C) Boxplots show the rotation errors of each method. In the boxplot, the center line denotes

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the median, box limits denote the upper and lower quartiles, and whiskers denote the  $1.5 \times$

682

interquartile range. (D) Boxplots show the translation errors of each method. In the boxplot, the

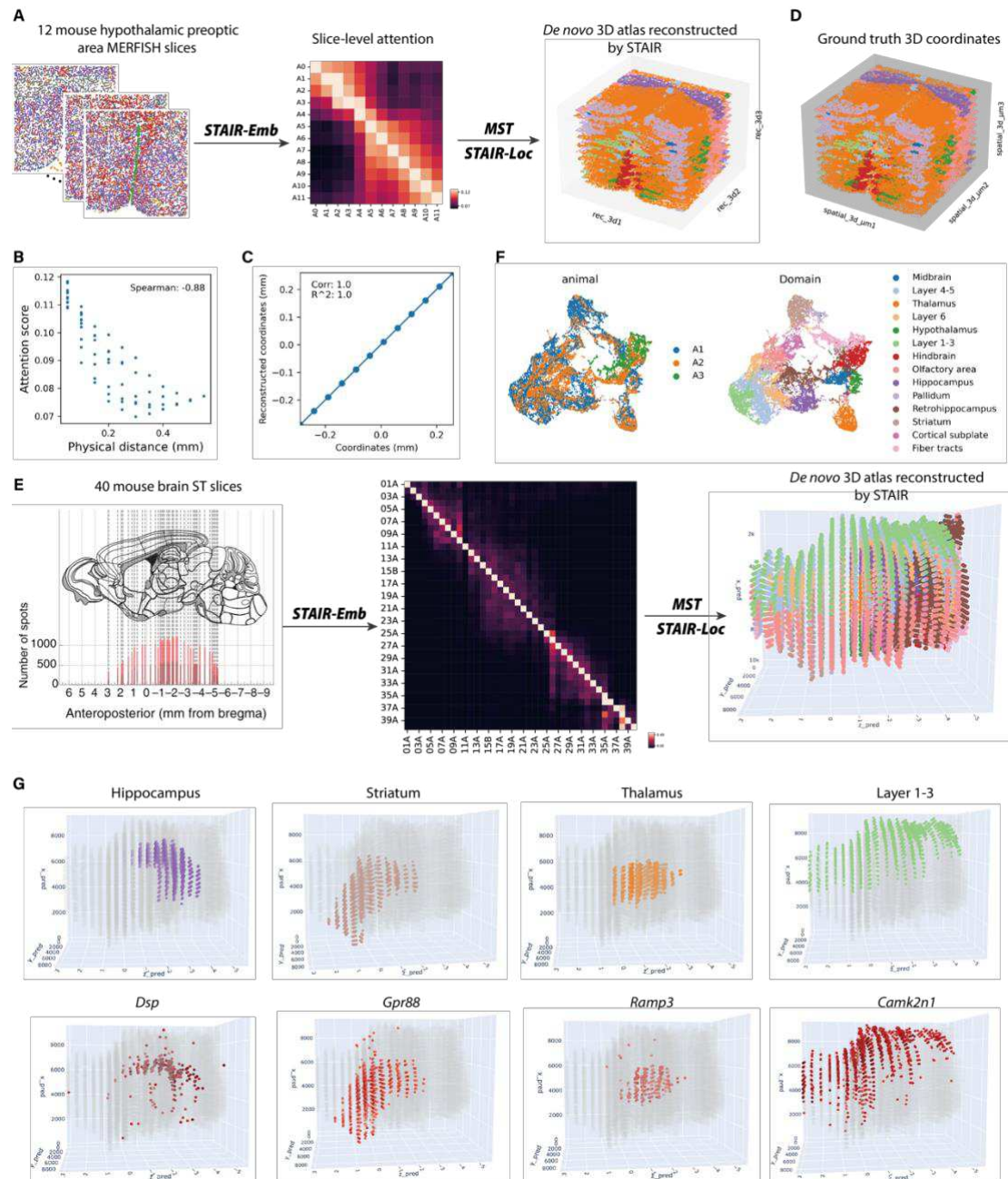
683

center line denotes the median, box limits denote the upper and lower quartiles, and whiskers denote

684

the  $1.5 \times$  interquartile range.

685



686

687 **Fig. 4. STAIR constructs *de novo* 3D atlas for the hypothalamic preoptic region and the mouse**

688 **brain. (A)** Diagram depicting the *de novo* 3D atlas reconstruction based on 12 MERFISH slices in

689 the hypothalamic preoptic region. We acquired slice-level attention scores by STAIR-Emb.

690 Subsequently, these attention scores were used for reconstructing distances along the parallel

691 direction of the slices. Finally, STAIR-Loc was employed to align the 2D coordinates guided by

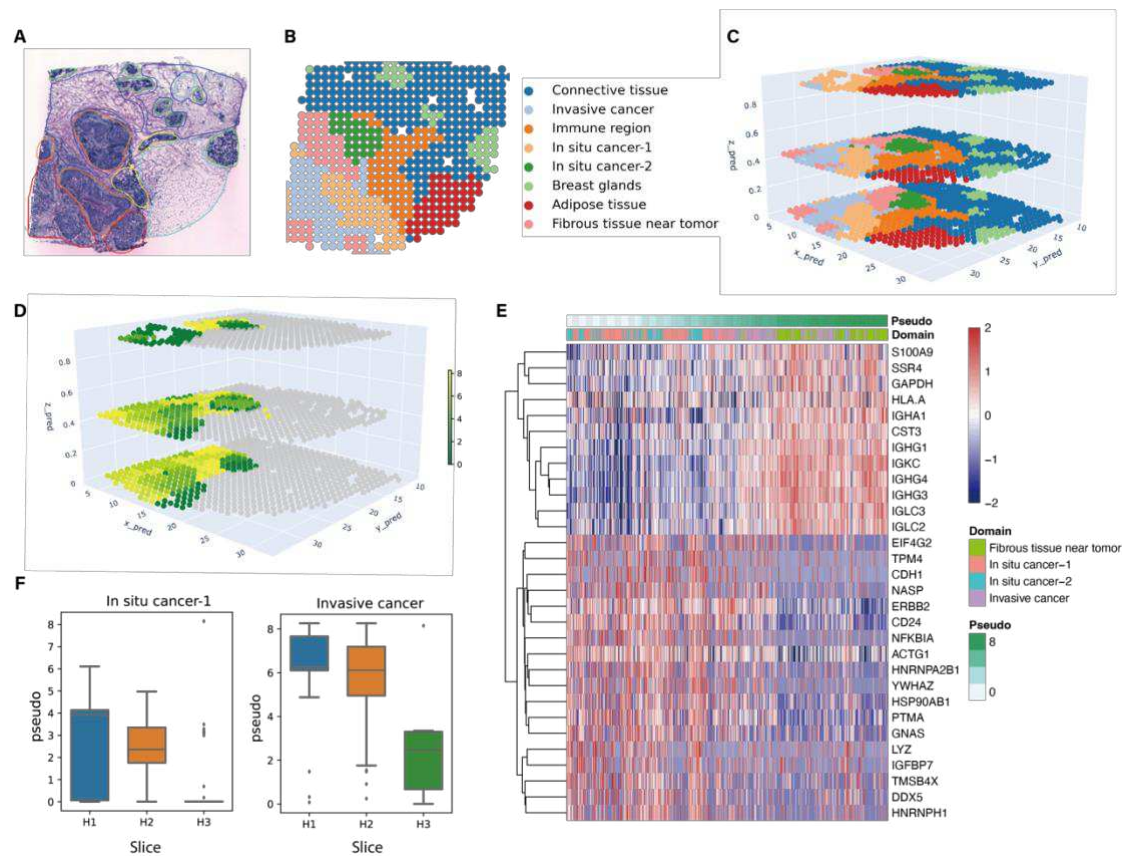
692 inter-slice distance. **(B)** Scatterplot showing the correlation between pairwise attention scores and

693 physical distance between slices, with a Spearman correlation coefficient of -0.88. **(C)** Comparing

694 reconstructed and actual physical coordinates in z-axis reveals a perfect correlation, with both the

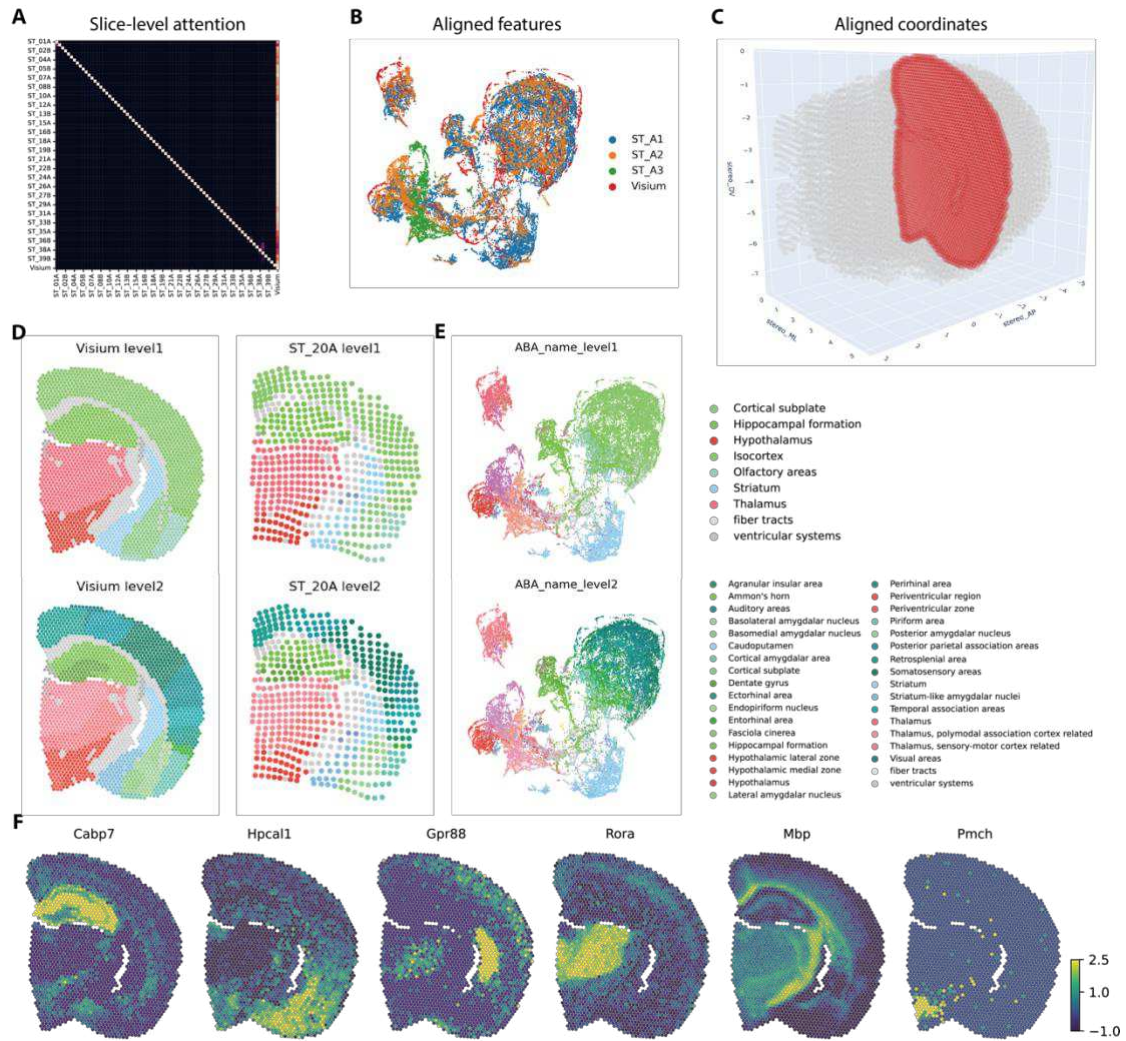
695 Pearson correlation coefficient and determination coefficient of 1. The reconstructed coordinates  
696 are proportionally scaled to match the dimensions of the real physical coordinates. **(D)** Visualization  
697 of ground truth 3D coordinates, colored by spatial domains. **(E)** Left: Distribution of 40 coronal  
698 sections generated by the ST platform used to generate the atlas, adapted from the Ortiz's work <sup>8</sup>.  
699 Middle: Heatmap of attention scores across 40 slices in the of ST mouse brain data. Right:  
700 Visualization of *de novo* reconstructed 3D coordinates, colored by spatial domains. **(F)** UMAP  
701 visualization generated by spatial embeddings of STAIR, colored by original samples (left) and  
702 domains (right). **(G)** Visualization of *de novo* reconstructed 3D coordinates, colored by spatial  
703 domains (top) and their corresponding marker genes (bottom).  
704





706

707 **Fig. 5. *De novo* 3D reconstruction and analysis of HER2+ breast cancer slices.** (A) Annotations  
 708 of slice H1 in the original study<sup>31</sup> into six distinct categories: invasive cancer (red), adipose tissue  
 709 (cyan), connective tissue (blue), breast glands (green), *in situ* cancer (orange) and immune infiltrates  
 710 (yellow). (B) 2D spatial visualization shows the domains identified by STAIR in slice H1. That of  
 711 the other two slices are displayed in Fig. S6B. (C) Visualization of *de novo* reconstructed 3D  
 712 coordinates, colored by spatial domains. (D) Pseudo-time of each spot inferred by Monocle3 based  
 713 on spatial embedding from STAIR. (E) Heatmap displaying genes with expression changes along  
 714 the Monocle-derived pseudo-time, with spots ordered by pseudo-time. (F) Boxplot shows the  
 715 pseudo-time of the spots in in situ cancer-1 (left) and invasive cancer (right) for each slice. In the  
 716 boxplot, the center line denotes the median, box limits denote the upper and lower quartiles, and  
 717 whiskers denote the  $1.5 \times$  interquartile range.



718

719 **Fig. 6. Assimilating new sections into a reference atlas. (A)** Heatmap depicting attention scores

720 among 41 mouse brain slices, including 40 slices of the reference atlas from the ST platform, along

721 with an additional slice generated from the Visium platform. **(B)** UMAP visualization of spatial

722 embedding generated by STAIR, with colors indicating the respective sample of origin. **(C)**

723 Visualization of the unified three-dimensional space after aligning the coordinates of the Visium

724 slice with the 3D atlas. Spots from the Visium slice and ST slices are shown in red and gray

725 respectively. **(D)** Spatial visualization of the Visium slice (left) and the ST slice (right) closest to

726 Visium slice, with colors indicating the anatomical regions of the first (top) and the second (bottom)

727 levels. **(E)** UMAP visualization of spatial embedding generated by STAIR, with colors indicating

728 the anatomical regions of the first (top) and second (bottom) levels. **(F)** Spatial visualization of

729 known regional marker genes.

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